Implicit differentiation example

A plot for the implicit relation $x^3 + y^2 + 3xy = 0$ is shown below.



- 1. The curve has two points corresponding to x = 2. Use the plot to estimate the y coordinate for each of these points.
- 2. Substitute x = 2 into the relation $x^3 + y^2 + 3xy = 0$. Solve the resulting equation to find the exact values of the y coordinate for each of these points.
- 3. Draw an estimated tangent line at each of the two points corresponding to x = 2. Estimate the slope of each line you draw.
- 4. Use implicit differentiation to compute the derivative $\frac{dy}{dx}$.
- 5. Evaluate $\frac{dy}{dx}$ for each of the two points corresponding to x = 2. Compare these values with the slopes you estimated in 3.